

Baryon-Strangeness Correlations

- Introduction
- BS and other correlations
- Some speculations

Work in collaboration with: A. Majumder and J. Randrup

Fluctuations in thermal system

e.g. Lattice QCD

$$Z = \text{Tr}[\exp(-\beta(H - \mu_Q Q - \mu_B B - \mu_S S))]$$

Mean :

$$\langle X \rangle = T \frac{\partial}{\partial \mu_X} \log(Z) = - \frac{\partial}{\partial \mu_X} F \quad X = Q, B, S$$

Variance:

$$\langle (\delta X)^2 \rangle = T^2 \frac{\partial^2}{\partial \mu_X^2} \log(Z) = -T \frac{\partial^2}{\partial \mu_X^2} F$$

Co-Variance:

$$\langle (\delta X)(\delta Y) \rangle = T^2 \frac{\partial^2}{\partial \mu_X \partial \mu_Y} \log(Z) = -T \frac{\partial^2}{\partial \mu_X \partial \mu_Y} F$$

Susceptibility:

$$\chi_{XY} = -\frac{1}{V} \frac{\partial^2}{\partial \mu_X \partial \mu_Y} F = -\frac{1}{V} \frac{\partial}{\partial \mu_X} \langle Y \rangle$$

Simple Observation

Or how can we test the sQGP

Simple QGP: strangeness is carried by strange quarks

→ Baryon Number and Strangeness are **correlated**

Hadron Gas: strangeness is carried mostly by mesons

→ Baryon Number and Strangeness are **uncorrelated**

Bound state QGP: strangeness is carried by partonic bound states

→ Baryon Number and Strangeness should be **uncorrelated**


$\langle BS \rangle$ and the Bound State QGP

Define:
$$C_{BS} \equiv -3 \frac{\langle (\delta B)(\delta S) \rangle}{\langle (\delta S)^2 \rangle} = -3 \frac{\langle (B - \langle B \rangle)(S - \langle S \rangle) \rangle}{\langle (S - \langle S \rangle)^2 \rangle} = -3 \frac{\langle BS \rangle}{\langle S^2 \rangle} = -3 \frac{X_{BS}}{X_{SS}}$$

In Experiment

$$C_{BS} = -3 \frac{\frac{1}{N_{eve.}} \sum_i B_i S_i - \frac{1}{N_{eve.}^2} \sum_i B_i \sum_j S_j}{\frac{1}{N_{eve.}} \sum_i S_i^2 - \frac{1}{N_{eve.}^2} \sum_i S_i \sum_j S_j}$$

(-3) compensates
baryon-number and
strangeness of quarks



Uncorrelated particles:

$$C_{BS} = -3 \frac{\sum_i \langle N_i \rangle S_i B_i}{\sum_i \langle N_i \rangle S_i^2}$$

Simple estimates

$$C_{BS} = \frac{-3\langle BS \rangle}{\langle S^2 \rangle}$$

In a QGP phase

$$-3\langle BS \rangle = \langle n_s \rangle + \langle n_{\bar{s}} \rangle$$

$$\langle S^2 \rangle = \langle n_s \rangle + \langle n_{\bar{s}} \rangle$$

At *all* T and μ

$$C_{BS} = 1$$

In hadron gas phase

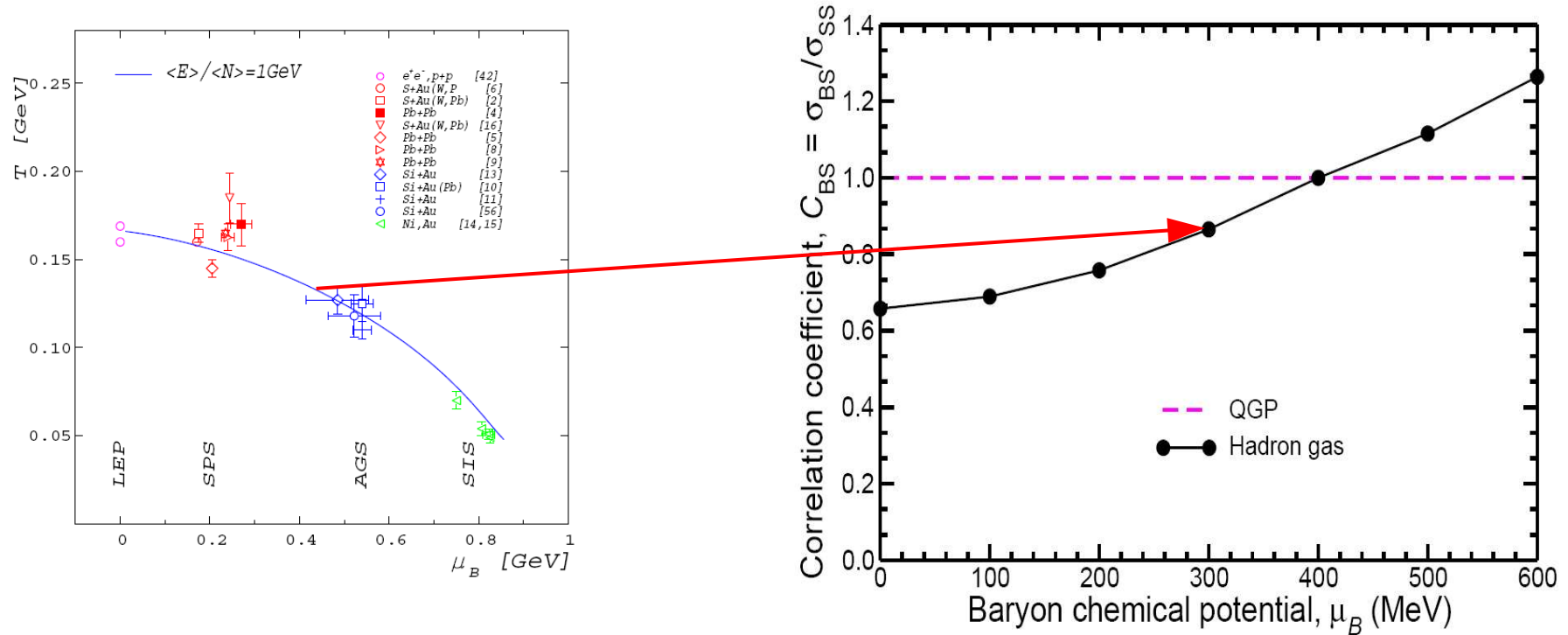
$$-3\langle BS \rangle = 3[\Lambda + \bar{\Lambda} + \Sigma + \bar{\Sigma} + \dots] \\ + 6[\Xi + \bar{\Xi} + \dots] + 9[\Omega + \dots]$$

$$\langle S^2 \rangle = K^+ + K^- + K^0 + \Lambda + \bar{\Lambda} + \dots$$

At T=170MeV, $\mu=0$

$$C_{BS} = 0.66$$

Hadron gas



At large μ : $N(K^+) = N(\Lambda + \Sigma)$

$$C_{BS} = 3 \frac{\Lambda + \Sigma}{K^+ + \Lambda + \Sigma} = \frac{3}{2} \quad \text{at large } \mu$$

The Bound State QGP

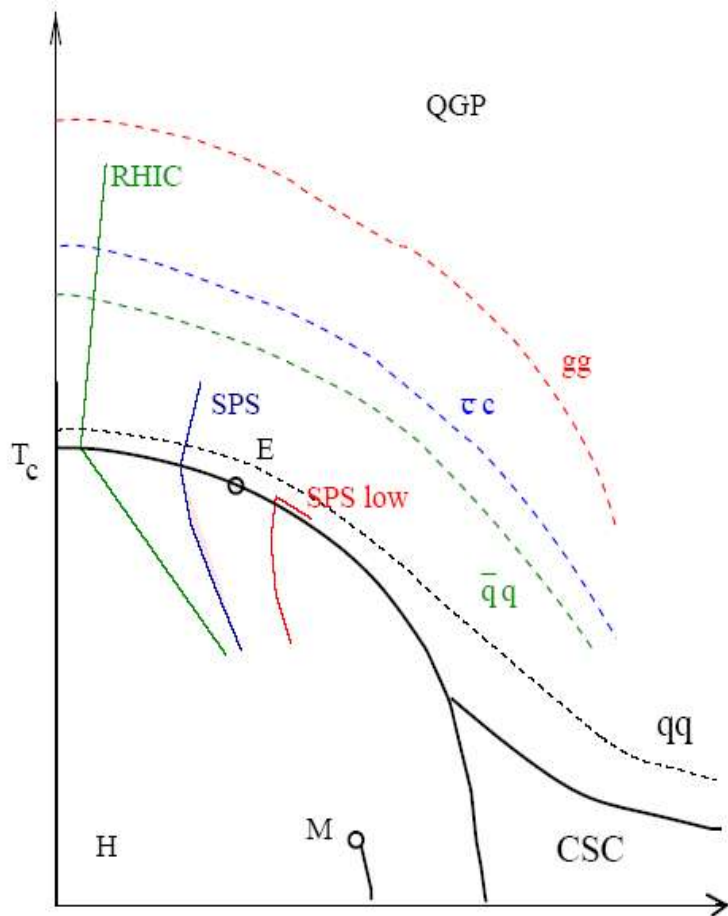


TABLE I. Binary attractive channels discussed in this work, the subscripts s , c , and f mean spin, color, and flavor; $N_f = 3$ is the number of relevant flavors.

Channel	Representation	Charge factor	No. of states
gg	1	$9/4$	9_s
gg	8	$9/8$	$9_s * 16$
$qg + \bar{q}g$	3	$9/8$	$3_c * 6_s * 2 * N_f$
$qg + \bar{q}g$	6	$3/8$	$6_c * 6_s * 2 * N_f$
$\bar{q}q$	1	1	$8_s * N_f^2$
$qq + \bar{q}\bar{q}$	3	$1/2$	$4_s * 3_c * 2 * N_f^2$

Gluon-Gluon states do not contribute!

C_{BS} in bound state QGP

- Heavy quark, antiquark quasiparticles: $C_{BS} = 1$
- Quark gluon states (color triplet, 36 states): $C_{BS} = 1$
- Quark-antiquark states: 8 π like, 24 ρ like: $C_{BS} = 0$

$$T=1.5T_c, C_{BS} = 0.61$$

Similar to Hadron gas estimate...

Estimates from the Lattice

$$\langle BS \rangle = \frac{T}{V} \frac{\partial}{\partial \mu_B} \frac{\partial}{\partial \mu_S} \log(Z)_{\mu_B=0} = X_{BS}$$

$$C_{BS} = -3 \frac{\langle BS \rangle}{\langle S^2 \rangle} = -3 \frac{\left\langle \frac{1}{3} (u+d+s)(-s) \right\rangle}{\langle S^2 \rangle} = \frac{X_{ss} + X_{us} + X_{ds}}{X_{ss}} = 1 + \frac{X_{us} + X_{ds}}{X_{ss}}$$

Calculated by (*quenched*): *R.V. Gavai, S. Gupta, Phys.Rev.D66:094510,2002*

At $T = 1.5 T_c$

$$X_{us} \approx X_{ds} \ll X_{ss}$$

$$C_{BS} = 1 + 0.00(3)/0.53(1)$$

Essential result: off-diagonal susceptibilities \ll diagonal susceptibilities

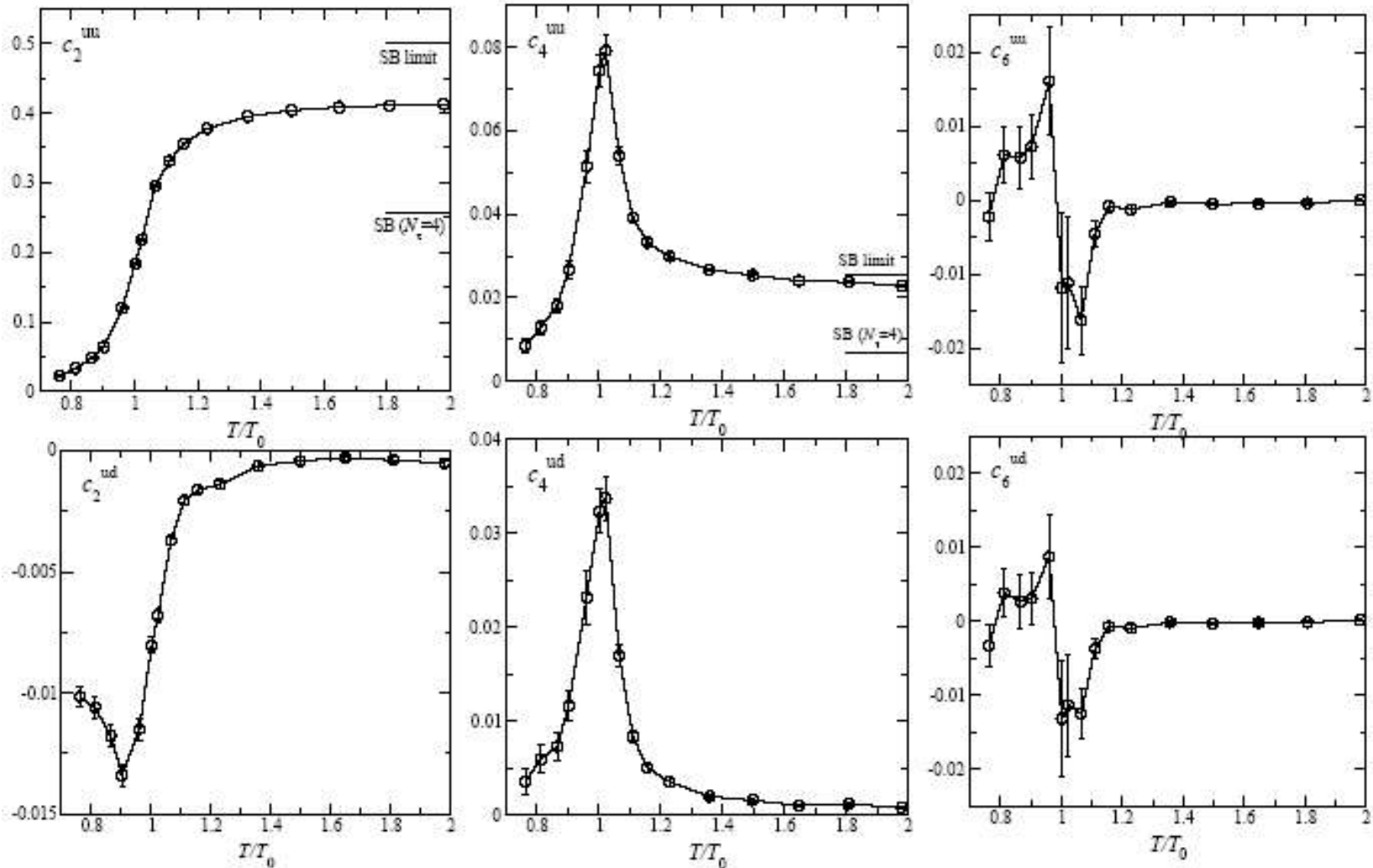
Results

- Hadron Gas $C_{BS} = 0.66$
- Bound State QGP $C_{BS} = 0.62$
- Independent quarks $C_{BS} = 1$
- Lattice QCD $C_{BS} = 1$

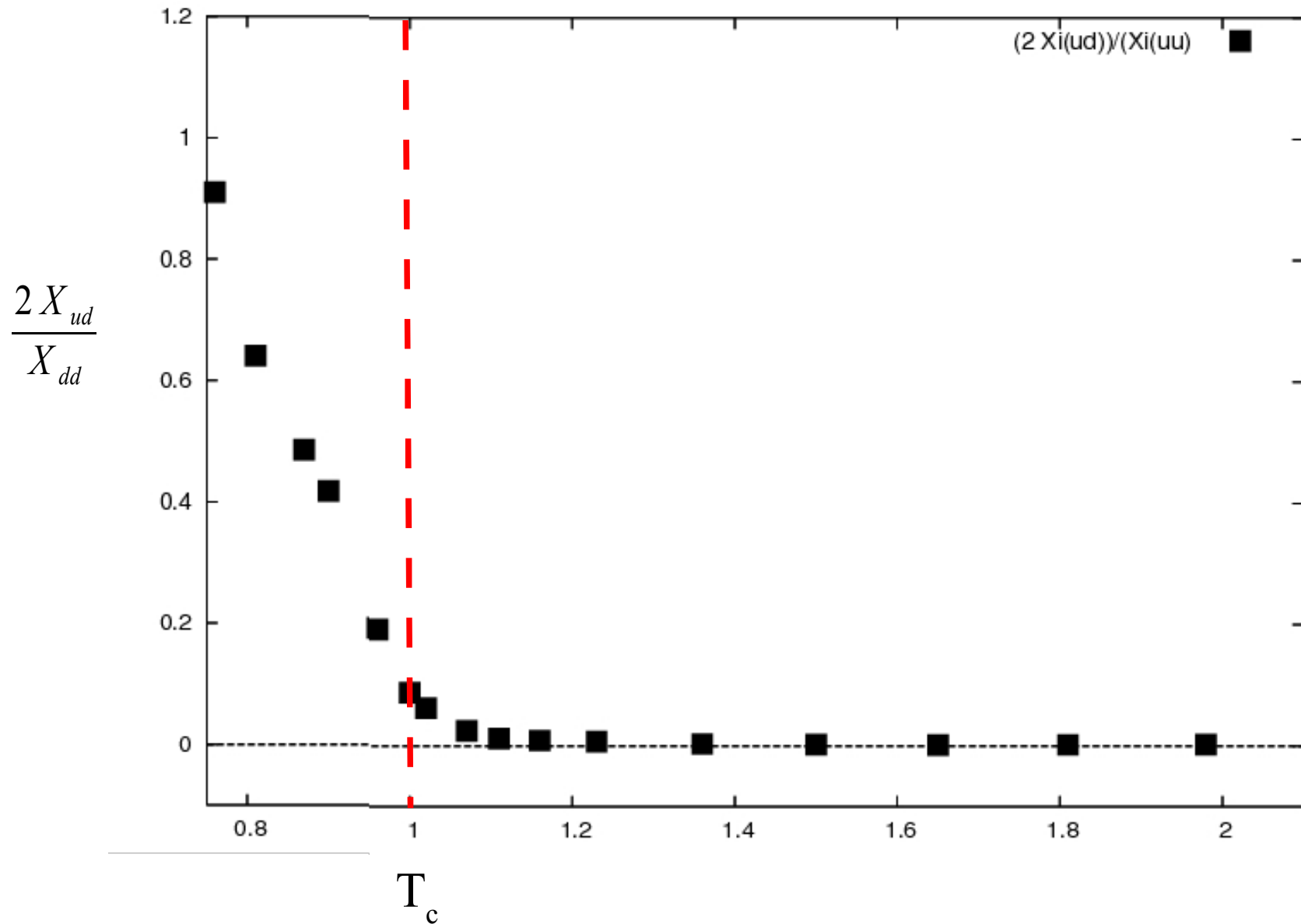
Full QCD, but with 2 flavors, gives similar insight!

From C.R. Alton et. al. Phys.Rev.D71:054508,2005

$$\frac{X(T, \mu_q)}{T^2} = 2c_2 + 12c_4 \left(\frac{\mu_q}{T}\right)^2 + 30c_6 \left(\frac{\mu_q}{T}\right)^4 + \dots$$



Ratio of Susceptibilities



Correlations and Lattice

(quenched) Lattice QCD:

$$X_{ud} = X_{us} = X_{ds} \approx 0$$

NO cross correlations among quark flavors!

quark – anti-quark bound states ?



Strongly interacting QGP??? Why are there no correlations?

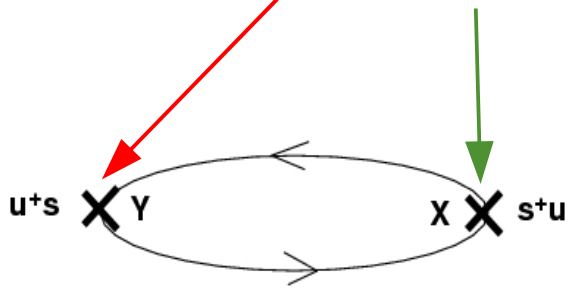


Quarks appear to be independent Quasi-Particles

Bound states and off-diagonal Susceptibilities

Correlator:

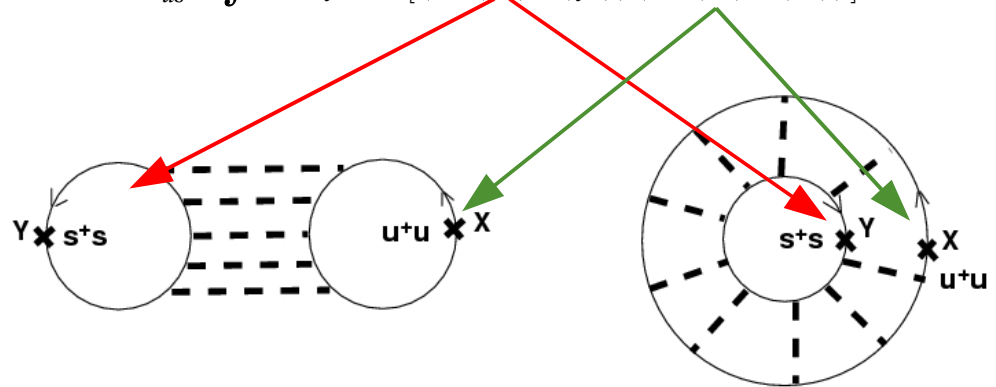
$$C(x, y) = \text{tr} [\rho(u^+(y)s(y)) (s^+(x)u(x))]$$



Measure for mass,
correlation length of
bound state

Susceptibility (χ_{us})

$$\chi_{us} = \int dx dy' \text{tr} [(s^+(y)s(y))(u^+(x)u(x))]$$



“Simply” counts number of
bound states

Some issues

- No statement about gluon bound states
- No statement about quark gluon bound states
- No statement about the heavy states (> 1.5 GeV) seen in correlation functions (Hatsuda et al, Karsch et al.)
 - Susceptibilities only measure the bulk!
 - Possibly collective modes ????? (G. Brown, QM 04)

Ways out...

- As many quark-quark states as quark-antiquark states
 - Not consistent with Shuryak model
 - Problem with charge - baryon-number correlations
- Large width of bound states
 - ~1 % correction is allowed by lattice
 - What is a bound state with large width?



Charge – Baryon Number Correlations

Consider:
$$C_{BQ} = \frac{\langle BQ \rangle}{\langle B^2 \rangle}$$

Lattice:

Di-quarks: $(uu), (dd), \frac{1}{2}(ud \pm du)$

$$C_{BQ} = \frac{2X_{uu} - X_{dd} + X_{ud}}{X_{uu} + X_{dd} + 2X_{ud}} = \frac{1}{2}$$

$$\langle BQ \rangle = \frac{2}{9}(4 - 2 + 2)N_{qq} = \frac{8}{9}N_{qq}$$

$$\langle B^2 \rangle = \frac{4}{9}N_{qq}$$

$$C_{BQ} = 2$$

NO di-quarks either!!!

Measuring R_{BS}

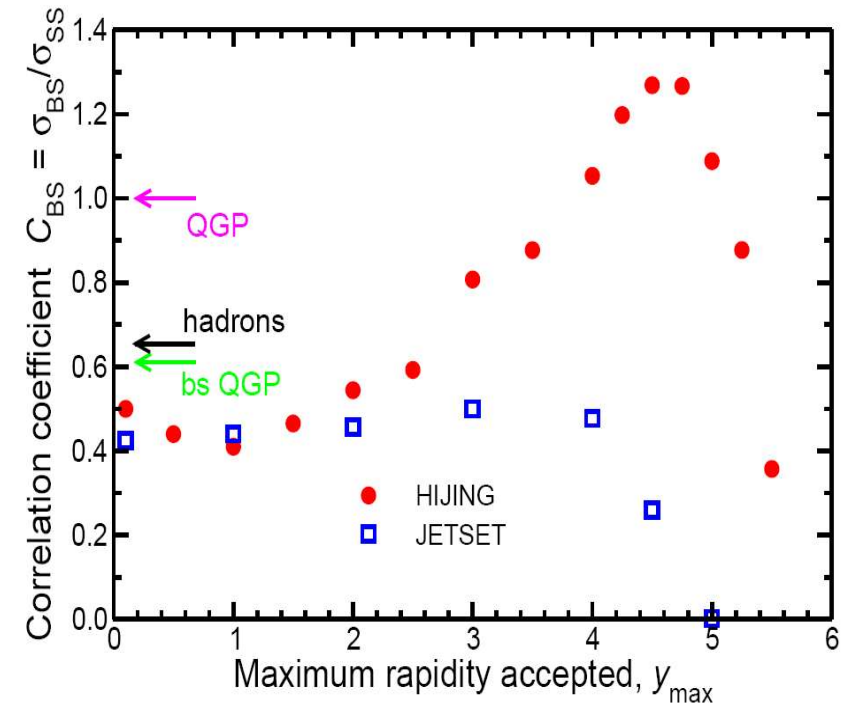
R_{BS} can be measured in principle

Advantages:

- Conserved quantities
- “Heavy” particles
- Less uncertainty due to hadronization

Issues:

- Baryon number (neutrons)
- Weak decay corrections for strangeness



Speculations!

- Lattice suggests a quasi-particle picture for QGP
 - Lattice EOS requires **massive** quasi-particle
 - This suggests a **repulsive** mean field (~ 500 MeV!!!)
 - A repulsive mean field generates **flow**!
 - RHIC data possibly consistent with **large** viscosity
-
- Alternative:
 - Glue has low viscosity and quarks tag along

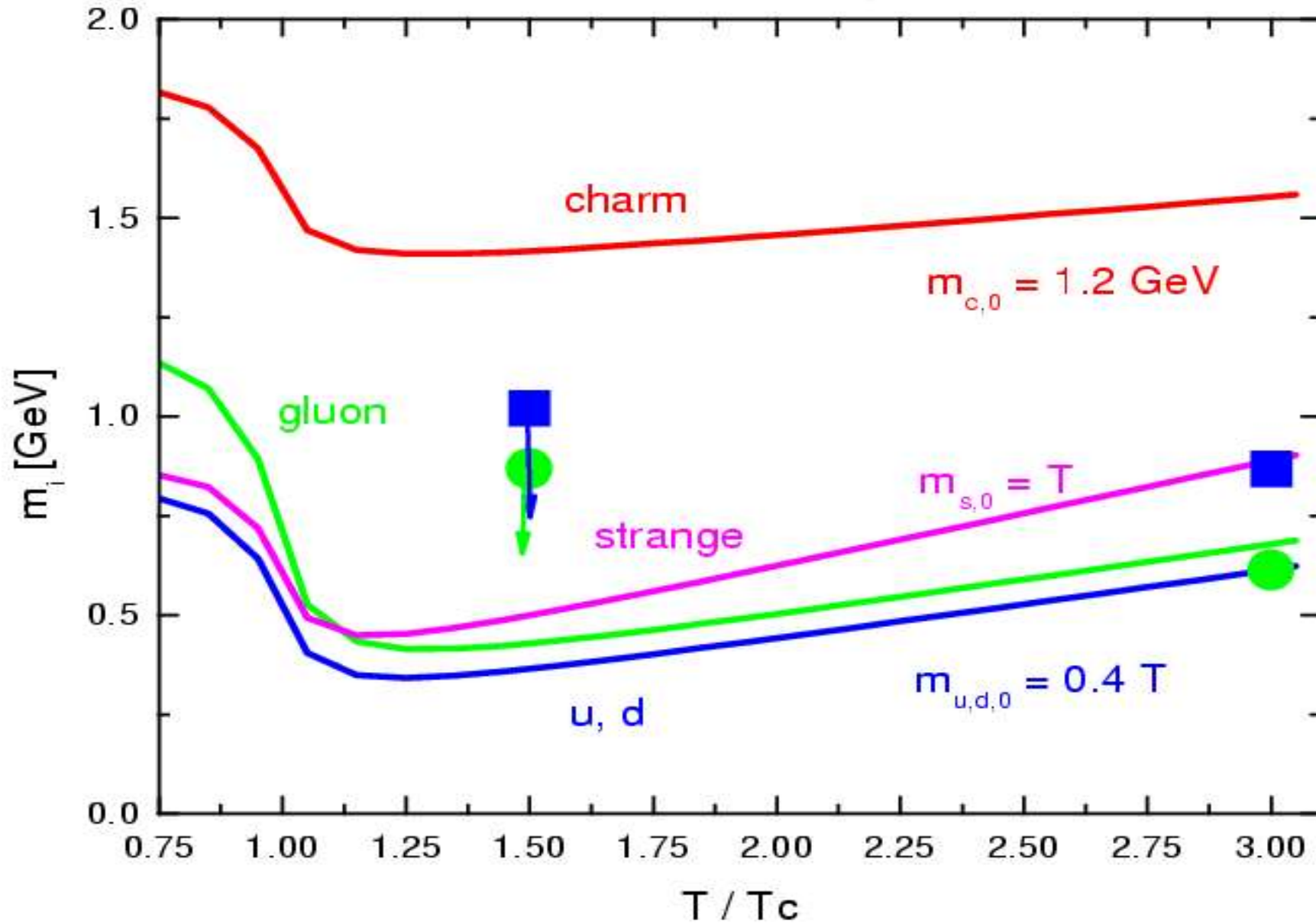
A. Peshier, B. Kampfer and G. Soff, Phys.Rev. D66:094003,2002.

J. P. Blaizot, E. Iancu and A. Rebhan, Phys.Rev. D63:065003,2001.

Summary

- BS correlation valuable diagnostic for structure of matter
- BS correlations impose strong limit on existence of bound states in the QCP
- Lattice QCD consistent with quasi-particle quarks
- Higher order “susceptibilities” need to be analyzed as well
- Mean field? Flow? High Viscosity? ?????

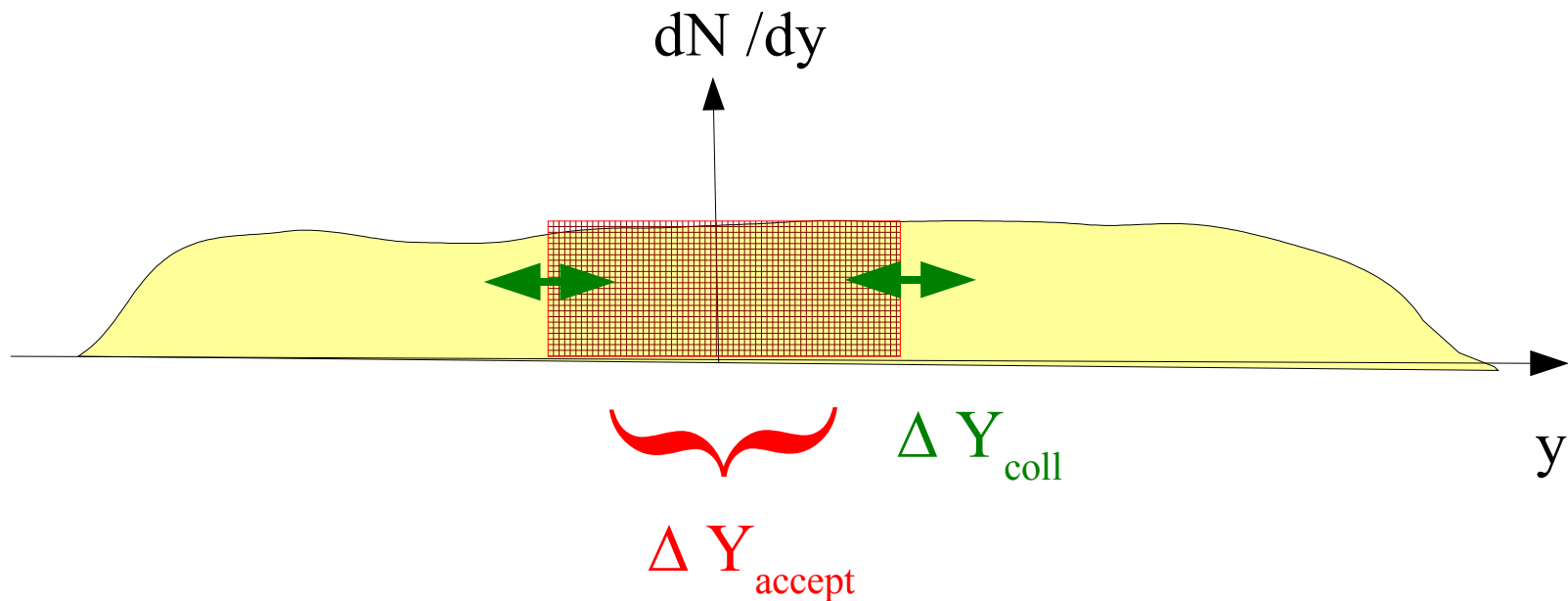
G^2 : fit to 2+1 Bielefeld data, $T_c = 170$ MeV



Fluctuations of conserved quantities

Quantum numbers conserved in Heavy ion collisions:

- Baryon number B (exactly)
- Charge Q (exactly)
- Strangeness S (almost!)
- Combinations are also conserved : BS , QS , BQ etc.



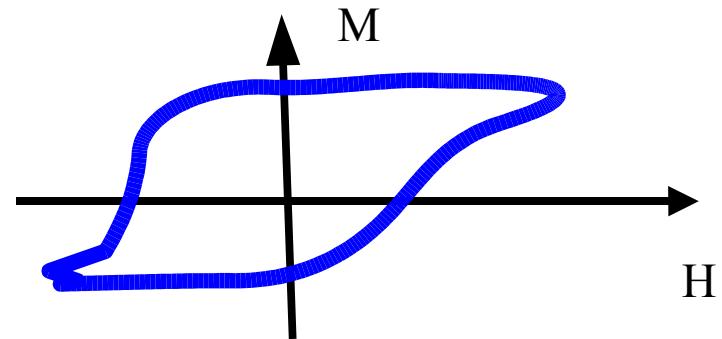
Condition for charge fluctuations: $\Delta Y_{\text{total}} \gg \Delta Y_{\text{accept}} \gg \Delta Y_{\text{coll}}$

Susceptibilities

$$E = E_0 + m H + \mu Q$$

$$\langle m \rangle = \frac{d F}{d H}$$

$$\langle Q \rangle = \frac{d F}{d \mu}$$



Susceptibilities

$$\chi_m = \frac{d^2 F}{d H^2}$$

$$\chi_Q = \frac{d^2 F}{d \mu^2}$$

$$\langle \delta m \rangle = \chi_m \delta H$$

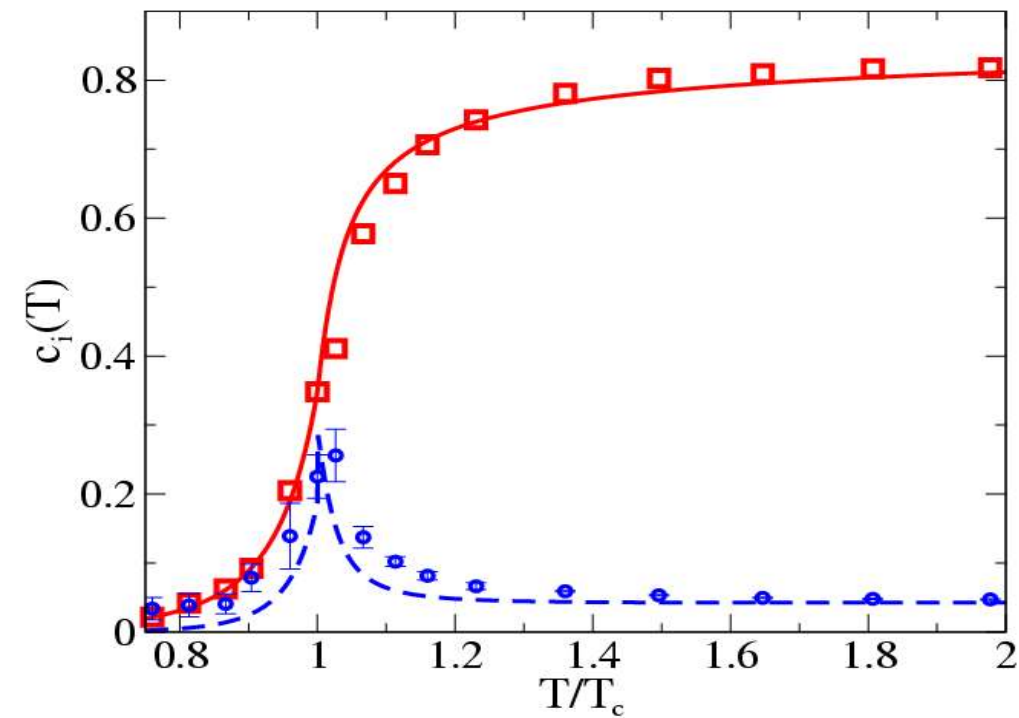
$$\langle \delta Q \rangle = \chi_Q \delta \mu$$

Linear response

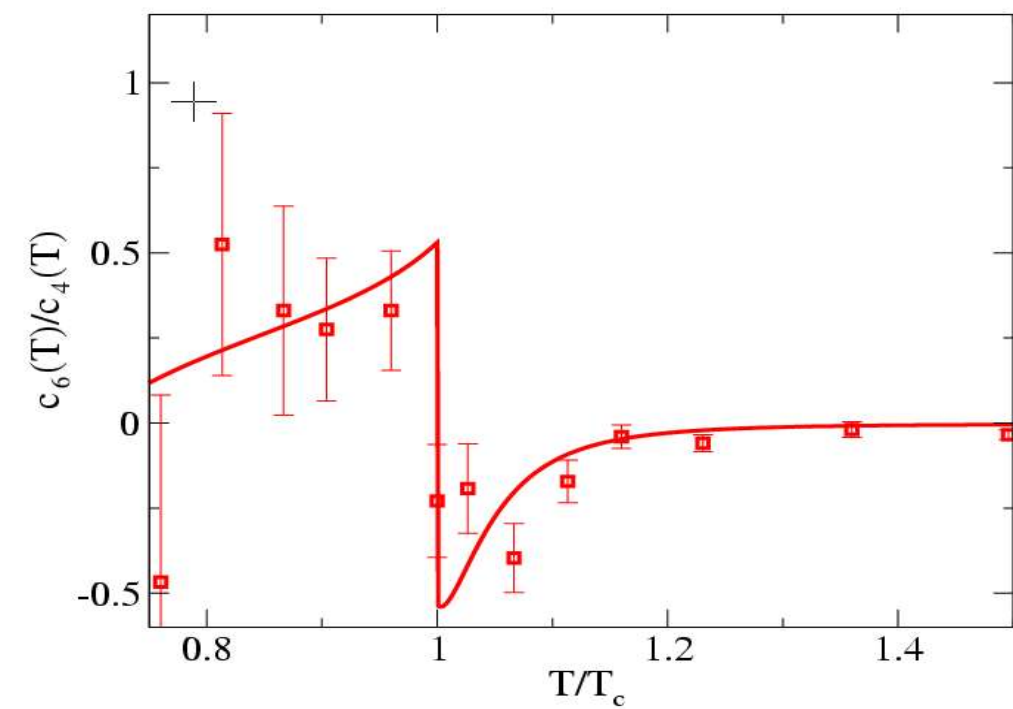
$$\langle (\delta m)^2 \rangle = \chi_m$$

$$\langle (\delta Q)^2 \rangle = \chi_Q$$

Fluctuations



Quasi-particle model by
Bluhm et al, hep-ph/0411106



Canonical QGP

vs.

Hadron gas

- **<BS>: strange quark and anti-quarks**
- **Strangeness carriers: strange quarks and anti-quarks**

- **<BS>: strange Baryons**
- **Strangeness carriers: Strange Baryons and Mesons**